

## Pure Mathematics P2 Mark scheme

Question	Scheme	Marks
<b>1(a)</b>	$f(x) = x^4 + x^3 + 2x^2 + ax + b$	
	Attempting $f(1)$ <b>or</b> $f(-1)$	M1
	$f(1) = 1 + 1 + 2 + a + b = 7$ <b>or</b> $4 + a + b = 7 \Rightarrow a + b = 3$ (as required) <b>AG</b>	A1* <b>cso</b>
		<b>(2)</b>
<b>(b)</b>	Attempting $f(-2)$ <b>or</b> $f(2)$	M1
	$f(-2) = 16 - 8 + 8 - 2a + b = -8 \Rightarrow -2a + b = -24$	A1
	Solving both equations simultaneously to get as far as $a = \dots$ <b>or</b> $b = \dots$	dM1
	Any one of $a = 9$ <b>or</b> $b = -6$	A1
	Both $a = 9$ and $b = -6$	A1
		<b>(5)</b>
<b>(7marks)</b>		
<b>Notes:</b>		
<p><b>(a)</b></p> <p><b>M1:</b> For attempting either <math>f(1)</math> or <math>f(-1)</math>.</p> <p><b>A1:</b> For applying <math>f(1)</math>, setting the result equal to 7, and manipulating this correctly to give the result given on the paper as <math>a + b = 3</math>. Note that the answer is given in part (a).</p> <p><b>Alternative</b></p> <p><b>M1:</b> For long division by <math>(x - 1)</math> to give a remainder in <math>a</math> and <math>b</math> which is independent of <math>x</math>.</p> <p><b>A1:</b> Or {Remainder = } <math>b + a + 4 = 7</math> leading to the correct result of <math>a + b = 3</math> (answer given).</p>		
<p><b>(b)</b></p> <p><b>M1:</b> Attempting either <math>f(-2)</math> or <math>f(2)</math>.</p> <p><b>A1:</b> <u>correct underlined equation</u> in <math>a</math> and <math>b</math>; e.g. <u><math>16 - 8 + 8 - 2a + b = -8</math></u> or equivalent, e.g. <math>-2a + b = -24</math>.</p> <p><b>dM1:</b> An attempt to eliminate one variable from 2 linear simultaneous equations in <math>a</math> and <math>b</math>. Note that this mark is dependent upon the award of the first method mark.</p> <p><b>A1:</b> Any one of <math>a = 9</math> or <math>b = -6</math>.</p> <p><b>A1:</b> Both <math>a = 9</math> and <math>b = -6</math> and a correct solution only.</p> <p><b>Alternative</b></p> <p><b>M1:</b> For long division by <math>(x + 2)</math> to give a remainder in <math>a</math> and <math>b</math> which is independent of <math>x</math>.</p> <p><b>A1:</b> For {Remainder = } <u><math>b - 2(a - 8) = -8</math></u> <math>\Rightarrow -2a + b = -24</math>.</p> <p>Then dM1A1A1 are applied in the same way as before.</p>		

Question	Scheme		Marks
<b>2(a)</b>	$S_{\infty} = \frac{20}{1 - \frac{7}{8}} ; = 160$	Use of a correct $S_{\infty}$ formula	M1
		160	A1
			<b>(2)</b>
<b>(b)</b>	$S_{12} = \frac{20\left(1 - \left(\frac{7}{8}\right)^{12}\right)}{1 - \frac{7}{8}} ; = 127.77324...$ $= 127.8$ (1 dp)	M1: Use of a correct $S_n$ formula with $n = 12$ (condone missing brackets around $\frac{7}{8}$ )	M1 A1
		A1: <b>awrt</b> 127.8	
			<b>(2)</b>
<b>(c)</b>	$160 - \frac{20\left(1 - \left(\frac{7}{8}\right)^N\right)}{1 - \frac{7}{8}} < 0.5$	Applies $S_N$ ( <b>GP only</b> ) with $a = 20$ , $r = \frac{7}{8}$ and “uses” 0.5 and their $S_{\infty}$ at any point in their working.	M1
	$160\left(\frac{7}{8}\right)^N < (0.5)$ or $\left(\frac{7}{8}\right)^N < \left(\frac{0.5}{160}\right)$	Attempt to isolate $+160\left(\frac{7}{8}\right)^N$ or $\left(\frac{7}{8}\right)^N$	dM1
	$N \log\left(\frac{7}{8}\right) < \log\left(\frac{0.5}{160}\right)$	Uses the law of logarithms to obtain an equation or an inequality of the form $N \log\left(\frac{7}{8}\right) < \log\left(\frac{0.5}{\text{their } S_{\infty}}\right)$ or $N > \log_{0.875}\left(\frac{0.5}{\text{their } S_{\infty}}\right)$	M1
	$N > \frac{\log\left(\frac{0.5}{160}\right)}{\log\left(\frac{7}{8}\right)} = 43.19823...$ <b>cso</b> $\Rightarrow N = 44$	$N = 44$ (Allow $N \geq 44$ but no $N > 44$ )	A1 cso
	An incorrect <b>inequality</b> statement at any stage in a candidate’s working loses the final mark. Some candidates do not realise that the direction of the inequality is reversed in the final line of their solution. <b>BUT</b> it is possible to gain full marks for using $=$ , as long as no incorrect working seen.		
			<b>(4)</b>
	<b>Alternative: Trial &amp; Improvement Method in (c):</b>		
	Attempts $160 - S_N$ or $S_N$ with at least one value for $N > 40$		M1
	Attempts $160 - S_N$ or $S_N$ with $N = 43$ or $N = 44$		dM1
	For evidence of examining $160 - S_N$ or $S_N$ for <b>both</b> $N = 43$ <b>and</b> $N = 44$ with <b>both</b> values correct to 2 DP Eg: $160 - S_{43} = \text{awrt } 0.51$ and $160 - S_{44} = \text{awrt } 0.45$ or $S_{43} = \text{awrt } 159.49$ and $S_{44} = \text{awrt } 159.55$		M1
	$N = 44$		A1 cso
	<b>Answer of <math>N = 44</math> only with no working scores no marks</b>		
			<b>(4)</b>
<b>(8 marks)</b>			

Question	Scheme	Marks												
3(a)	<table><tr><td><math>x</math></td><td>0</td><td>0.25</td><td>0.5</td><td>0.75</td><td>1</td></tr><tr><td><math>y</math></td><td>1</td><td>1.251</td><td>1.494</td><td>1.741</td><td>2</td></tr></table>	$x$	0	0.25	0.5	0.75	1	$y$	1	1.251	1.494	1.741	2	B1 B1
	$x$	0	0.25	0.5	0.75	1								
$y$	1	1.251	1.494	1.741	2									
		(2)												
(b)	$\frac{1}{2} \times 0.25, \{(1 + 2) + 2(1.251 + 1.494 + 1.741)\}$ o.e.	B1 M1 A1ft												
	= 1.4965	A1												
		(4)												
(c)	Gives any valid reason including <ul style="list-style-type: none"><li>• Decrease the width of the strips</li><li>• Use more trapezia</li><li>• Increase the number of strips</li></ul> Do not accept use more decimal places	B1												
		(1)												
(7 marks)														
Notes:														
(a)														
B1: For 1.494														
B1: For 1.741 (1.740 is B0). Wrong accuracy e.g. 1.49, 1.74 is B1B0														
(b)														
B1: Need $\frac{1}{2}$ of 0.25 or 0.125 o.e.														
M1: Requires first bracket to contain first plus last values <b>and</b> second bracket to include no additional values from the three in the table. If the only mistake is to omit one value from second bracket this may be regarded as a slip and <b>M</b> mark can be allowed ( An extra repeated term forfeits the <b>M</b> mark however) $x$ values: <b>M0</b> if values used in brackets are $x$ values instead of $y$ values														
A1ft: Follows their answers to part (a) and is for {correct expression}														
A1: Accept 1.4965, 1.497, or 1.50 only after correct work. (No follow through except one special case below following 1.740 in table).														
Separate trapezia may be used: <b>B1</b> for 0.125, <b>M1</b> for $\frac{1}{2}h(a+b)$ used 3 or 4 times (and <b>A1ft</b> if it is all correct) e.g. $0.125(1+ 1.251) + 0.125(1.251+1.494) + 0.125(1.741 + 2)$ is <b>M1 A0</b> equivalent to missing one term in { } in main scheme.														

Question	Scheme	Marks																												
4	<p><b>A solution based around a table of results</b></p> <table><tr><td><math>n</math></td><td><math>n^2</math></td><td><math>n^2 + 2</math></td><td></td></tr><tr><td>1</td><td>1</td><td>3</td><td>Odd</td></tr><tr><td>2</td><td>4</td><td>6</td><td>Even</td></tr><tr><td>3</td><td>9</td><td>11</td><td>Odd</td></tr><tr><td>4</td><td>16</td><td>18</td><td>Even</td></tr><tr><td>5</td><td>25</td><td>27</td><td>Odd</td></tr><tr><td>6</td><td>36</td><td>38</td><td>Even</td></tr></table>	$n$	$n^2$	$n^2 + 2$		1	1	3	Odd	2	4	6	Even	3	9	11	Odd	4	16	18	Even	5	25	27	Odd	6	36	38	Even	
$n$	$n^2$	$n^2 + 2$																												
1	1	3	Odd																											
2	4	6	Even																											
3	9	11	Odd																											
4	16	18	Even																											
5	25	27	Odd																											
6	36	38	Even																											
	When $n$ is odd, $n^2$ is odd (odd $\times$ odd = odd) so $n^2 + 2$ is also odd	M1																												
	So for all odd numbers $n$ , $n^2 + 2$ is also odd and so cannot be divisible by 4 (as all numbers in the 4 times table are even)	A1																												
	When $n$ is even, $n^2$ is even <b>and a multiple</b> of 4, so $n^2 + 2$ cannot be a multiple of 4	M1																												
	Fully correct and exhaustive proof. Award for both of the cases above plus a final statement "So for all $n$ , $n^2 + 2$ cannot be divisible by 4"	A1*																												
		(4)																												
	<b>Alternative - (algebraic) proof</b>																													
	If $n$ is even, $n = 2k$ , so $\frac{n^2 + 2}{4} = \frac{(2k)^2 + 2}{4} = \frac{4k^2 + 2}{4} = k^2 + \frac{1}{2}$	M1																												
	If $n$ is odd, $n = 2k + 1$ , so $\frac{n^2 + 2}{4} = \frac{(2k + 1)^2 + 2}{4} = \frac{4k^2 + 4k + 3}{4} = k^2 + k + \frac{3}{4}$	M1																												
	For a partial explanation stating that <ul style="list-style-type: none"><li>either of <math>k^2 + \frac{1}{2}</math> or <math>k^2 + k + \frac{3}{4}</math> are not a whole numbers.</li><li>with some valid reason stating why this means that <math>n^2 + 2</math> is not a multiple of 4.</li></ul>	A1																												
	Full proof with no errors or omissions. This must include <ul style="list-style-type: none"><li>The conjecture</li><li>Correct notation and algebra for both even and odd numbers</li><li>A full explanation stating why, for all <math>n</math>, <math>n^2 + 2</math> is not divisible by 4</li></ul>	A1*																												
		(4)																												
(4 marks)																														

Question	Scheme		Marks
<b>5(a)</b>	$(S=)a + (a + d) + \dots + [a+(n-1)d]$	B1: requires at least 3 terms, must include first and last terms, an adjacent term and dots!	B1
	$(S=)[a+(n-1)d] + \dots + a$	M1: for reversing series (dots needed)	M1
	$2S = [2a+(n-1)d] + \dots + [2a+(n-1)d]$	dM1: for adding, must have $2S$ and be a genuine attempt. Either line is sufficient. Dependent on 1 <sup>st</sup> M1.	dM1
	$2S = n[2a+(n-1)d]$ $S = \frac{n}{2} [2a+(n-1)d]$ cso	(NB – Allow first 3 marks for use of $l$ for last term but as given for final mark )	A1
			<b>(4)</b>
<b>(b)</b>	$600 = 200 + (N-1)20 \Rightarrow N = \dots$	Use of 600 with a <b>correct</b> formula in an attempt to find $N$ .	M1
	$N = 21$	cso	A1
			<b>(2)</b>
<b>(c)</b>	<b>Look for an AP first:</b>		
	$S = \frac{21}{2} (2 \times 200 + 20 \times 20)$ <b>or</b> $\frac{21}{2} (200 + 600)$	M1: Use of correct sum formula with their <b>integer</b> $n = N$ or $N - 1$ from part (b) where $3 < N < 52$ and $a = 200$ and $d = 20$ .	M1A1
	$S = \frac{20}{2} (2 \times 200 + 19 \times 20)$ <b>or</b> $\frac{20}{2} (200 + 580)$ (= 8400 <b>or</b> 7800)	M1: Use of correct sum formula with their <b>integer</b> $n = N$ or $N - 1$ from part (b) where $3 < N < 52$ and $a = 200$ and $d = 20$ .	
	<b>Then for the constant terms:</b>		
	$600 \times (52 - "N") (= 18600)$	M1: $600 \times k$ where $k$ is an integer and $3 < k < 52$	M1
		A1: A correct un-simplified follow through expression with their $k$ consistent with $n$ so that $n + k = 52$	A1ft
	So total is 27000	<b>cao</b>	A1
	<b>There are no marks in (c) for just finding <math>S_{52}</math></b>		
			<b>(5)</b>
	<b>(11 marks)</b>		

Question	Scheme		Marks
<b>6(i)</b>	$\log_2\left(\frac{2x}{5x+4}\right) = -3$ or $\log_2\left(\frac{5x+4}{2x}\right) = 3$ or $\log_2\left(\frac{5x+4}{x}\right) = 4$		M1
	$\left(\frac{2x}{5x+4}\right) = 2^{-3}$ or $\left(\frac{5x+4}{2x}\right) = 2^3$ or $\left(\frac{5x+4}{x}\right) = 2^4$		M1
	$16x = 5x + 4 \Rightarrow x =$ (depends on Ms and must be this equation or equiv)		dM1
	$x = \frac{4}{11}$ or exact recurring decimal 0.36 after correct work		A1 cso
	<b>Alternative</b>		
	$\log_2(2x) + 3 = \log_2(5x + 4)$		
	So $\log_2(2x) + \log_2(8) = \log_2(5x + 4)$ earns 2 <sup>nd</sup> M1 (3 replaced by $\log_2 8$ )		2 <sup>nd</sup> M1
	Then $\log_2(16x) = \log_2(5x + 4)$ earns 1 <sup>st</sup> M1 (addition law of logs)		1 <sup>st</sup> M1
	Then final M1 A1 as before		dM1A1
			<b>(4)</b>
<b>(ii)</b>	$\log_a y + \log_a 2^3 = 5$		M1
	$\log_a 8y = 5$	Applies product law of logarithms	dM1
	$y = \frac{1}{8}a^5$ <b>cso</b>	$y = \frac{1}{8}a^5$ <b>cso</b>	A1
			<b>(3)</b>
<b>(7 marks)</b>			
<b>Notes:</b>			
<b>(i)</b>			
<b>M1:</b> Applying the subtraction or addition law of logarithms correctly to make <b>two log terms into one</b> log term .			
<b>M1:</b> For RHS of either $2^{-3}$ , $2^3$ , $2^4$ or $\log_2\left(\frac{1}{8}\right)$ , $\log_2 8$ or $\log_2 16$ i.e. using connection between log base 2 and 2 to a power. This may follow an error. <b>Use of <math>3^2</math> is M0</b>			
<b>dM1:</b> Obtains <b>correct</b> linear equation in $x$ . usually the one in the scheme and attempts $x =$			
<b>A1:</b> <b>cso</b> . Answer of $4/11$ with <b>no</b> suspect log work preceding this.			
<b>(ii)</b>			
<b>M1:</b> Applies power law of logarithms to replace $3\log_a 2$ by $\log_a 2^3$ or $\log_a 8$			
<b>dM1:</b> (Should not be following M0) Uses addition law of logs to give $\log_a 2^3 y = 5$ or $\log_a 8y = 5$			

Question	Scheme	Marks
<b>7(a)</b>	Obtain $(x \pm 10)^2$ <b>and</b> $(y \pm 8)^2$	M1
	$(10, 8)$	A1
		<b>(2)</b>
<b>(b)</b>	See $(x \pm 10)^2 + (y \pm 8)^2 = 25 (= r^2)$ <b>or</b> $(r^2 =) "100" + "64" - 139$	M1
	$r = 5^*$	A1
		<b>(2)</b>
<b>(c)</b>	Substitute $x = 13$ into the equation of circle and solve quadratic to give $y =$ e.g. $x = 13 \Rightarrow (13 - 10)^2 + (y - 8)^2 = 25 \Rightarrow (y - 8)^2 = 16$ so $y = 4$ <b>or</b> $12$	M1
	<b>N.B. This can be attempted via a 3, 4, 5 triangle so spotting this and achieving one value for y is M1 A1. Both values scores M1 A1 A1</b>	A1 A1
		<b>(3)</b>
<b>(d)</b>	$OC = \sqrt{10^2 + 8^2} = \sqrt{164}$	M1
	Length of tangent $= \sqrt{164 - 5^2} = \sqrt{139}$	M1 A1
		<b>(3)</b>

**(10 marks)**

**Notes:**

**(a)**

**M1:** Obtains  $(x \pm 10)^2$  **and**  $(y \pm 8)^2$  May be implied by one correct coordinate

**A1:**  $(10, 8)$  Answer only scores both marks.

**Alternative: Method 2:** From  $x^2 + y^2 + 2gx + 2fy + c = 0$  centre is  $(\pm g, \pm f)$

**M1:** Obtains  $(\pm 10, \pm 8)$

**A1:** Centre is  $(-g, -f)$ , **and so centre is**  $(10, 8)$ .

**(b)**

**M1:** For a correct method leading to  $r = \dots$ , or  $r^2 =$

Allow  $"100" + "64" - 139$  or an attempt at using  $(x \pm 10)^2 + (y \pm 8)^2 = r^2$  form to identify  $r =$

**A1\*:**  $r = 5$  This is a printed answer, so a correct method must be seen.

**Alternative:**

**(b)**

**M1:** Attempts to use  $\sqrt{g^2 + f^2 - c}$  or  $(r^2 =) "100" + "64" - 139$

**A1\*:**  $r = 5$  following a correct method.

**(c)**

**M1:** Substitutes  $x = 13$  into either form of the circle equation, forms and solves the quadratic equation in  $y$

**A1:** Either  $y = 4$  **or**  $12$

**A1:** Both  $y = 4$  **and**  $12$

**Question 7 notes** *continued*

**(d)**

**M1:** Uses Pythagoras' Theorem to find length OC using their (10,8)

**M1:** Uses Pythagoras' Theorem to find  $OX$ . Look for  $\sqrt{OC^2 - r^2}$

**A1:**  $\sqrt{139}$  only



Question	Scheme	Marks
8(a)	Substitutes $x = 1$ in $C_1: y = 10x - x^2 - 8 = 10 - 1 - 8 = 1$ and in $C_2: y = x^3 = 1^3 = 1 \Rightarrow (1, 1)$ lies on both curves.	B1
		(1)
(b)	$10x - x^2 - 8 = x^3$ $x^3 + x^2 - 10x + 8 = 0$	B1
	$(x - 1)(x^2 + 2x - 8) = 0$	M1 A1
	$(x - 1)(x + 4)(x - 2) = 0 \quad x = 2$	M1 A1
	$(2, 8)$	A1
		(6)
(c)	$\int \{(10x - x^2 - 8) - x^3\} dx$	M1
	$= 5x^2 - \frac{x^3}{3} - 8x - \frac{x^4}{4}$	M1 A1
	Using limits 2 and 1: $\left(20 - \frac{8}{3} - 16 - 4\right) - \left(5 - \frac{1}{3} - 8 - \frac{1}{4}\right)$	M1
	$= \frac{11}{12}$	A1
		(5)
(12 marks)		
Notes:		
(a)		
B1:	Substitutes $x$ into both $y = 10x - x^2 - 8$ and $y = x^3$ <b>AND</b> achieves $y = 1$ in both.	
(b)		
B1:	Sets equations equal to each other and proceeds to $x^3 + x^2 - 10x + 8 = 0$	
M1:	Divides by $(x - 1)$ to form a quadratic factor. Allow any suitable algebraic method including division or inspection.	
A1:	Correct quadratic factor $(x^2 + 2x - 8)$	
M1:	For factorising of their quadratic factor.	
A1:	Achieves $x = 2$	
A1:	Coordinates of $B = (2, 8)$	
(c)		
M1:	For knowing that the area of $R = \int \{(10x - x^2 - 8) - x^3\} dx$	
	This may also be scored for finding separate areas and subtracting.	
M1:	For raising the power of $x$ seen in at least three terms.	
A1:	Correct integration. It may be left un-simplified. That is allow $\frac{10x^2}{2}$ for $5x^2$	

**Question 8 notes** *continued*

**M1:** For using the limits "2" and 1 in their integrated expression. If separate areas have been attempted, "2" and 1 must be used in both integrated expressions.

**A1:** For  $\frac{11}{12}$  or exact equivalent.

Question	Scheme		Marks
9(i)	<b>Way 1</b> Divides by $\cos 3\theta$ to give $\tan 3\theta = \sqrt{3}$ so $\Rightarrow (3\theta) = \frac{\pi}{3}$	<b>Way 2</b> Or Squares both sides, uses $\cos^2 3\theta + \sin^2 3\theta = 1$ , obtains $\cos 3\theta = \pm \frac{1}{2}$ or $\sin 3\theta = \pm \frac{\sqrt{3}}{2}$  so $(3\theta) = \frac{\pi}{3}$	M1
	Adds $\pi$ or $2\pi$ to previous value of angle( to give $\frac{4\pi}{3}$ or $\frac{7\pi}{3}$ )		M1
	So $\theta = \frac{\pi}{9}, \frac{4\pi}{9}, \frac{7\pi}{9}$ (all three, no extra in range)		A1
			(3)
(ii)(a)	$4(1 - \cos^2 x) + \cos x = 4 - k$	Applies $\sin^2 x = 1 - \cos^2 x$	M1
	Attempts to solve $4 \cos^2 x - \cos x - k = 0$ , to give $\cos x =$		dM1
	$\cos x = \frac{1 \pm \sqrt{1+16k}}{8}$ or $\cos x = \frac{1}{8} \pm \sqrt{\frac{1}{64} + \frac{k}{4}}$  or other correct equivalent		A1
			(3)
(b)	$\cos x = \frac{1 \pm \sqrt{49}}{8} = 1$ and $-\frac{3}{4}$ (see the note below if errors are made)		M1
	Obtains two solutions from 0 , 139 , 221 (0 or 2.42 or 3.86 in radians)		dM1
	$x = 0$ and 139 and 221 (allow awrt 139 and 221) must be in degrees		A1
			(3)
(9 marks)			
Notes:			
(i)			
<b>M1:</b> Obtains $\frac{\pi}{3}$ . Allow $x = \frac{\pi}{3}$ or even $\theta = \frac{\pi}{3}$ . Need not see working here. May be implied by  $\theta = \frac{\pi}{9}$ in final answer (allow $(3\theta) = 1.05$ or $\theta = 0.349$ as decimals or $(3\theta) = 60$ or $\theta = 20$ as degrees for this mark). Do not allow $\tan 3\theta = -\sqrt{3}$ nor $\tan 3\theta = \pm \frac{1}{\sqrt{3}}$			
<b>M1:</b> Adding $\pi$ or $2\pi$ to a previous value however obtained. It is not dependent on the previous mark. (May be implied by final answer of $\theta = \frac{4\pi}{9}$ or $\frac{7\pi}{9}$ ). This mark may also be given for answers as decimals [4.19 or 7.33], or degrees (240 or 420).			

**Question 9 notes** *continued*

**A1:** Need all three correct answers in terms of  $\pi$  and **no extras in range**.

**NB:**  $\theta = 20^\circ, 80^\circ, 140^\circ$  earns **M1M1A0** and **0.349, 1.40 and 2.44** earns **M1M1A0**

**(ii)(a)**

**M1:** Applies  $\sin^2 x = 1 - \cos^2 x$  (allow even if brackets are missing e.g.  $4 \times 1 - \cos^2 x$ ).  
This must be awarded in (ii) (a) for an expression with  $k$  not after  $k = 3$  is substituted.

**dM1:** Uses formula or completion of square to obtain  $\cos x =$  expression in  $k$   
(Factorisation attempt is M0)

**A1:** cao - award for their final simplified expression

**(ii)(b)**

**M1:** **Either** attempts to substitute  $k = 3$  into their answer to obtain two values for  $\cos x$   
**Or** restarts with  $k = 3$  to find two values for  $\cos x$  (They cannot earn marks in ii(a) for this). **In both cases** they need to have applied  $\sin^2 x = 1 - \cos^2 x$  (brackets may be missing) **and** correct method for solving their quadratic (usual rules – see notes) The values for  $\cos x$  may be  $>1$  or  $<-1$ .

**dM1:** Obtains **two correct** values for  $x$

**A1:** Obtains **all three correct values** in degrees (allow awrt 139 and 221) including 0.  
Ignore excess answers outside range (including 360 degrees) Lose this mark for excess answers in the range or radian answers.